



When Pull Turns to Shove

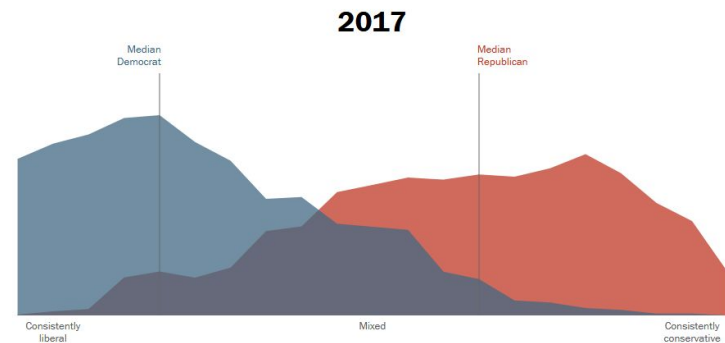
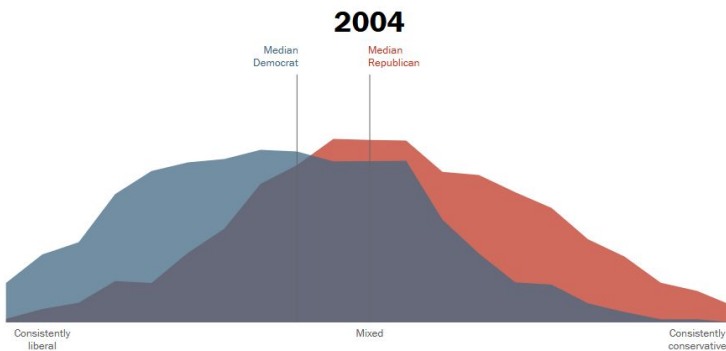
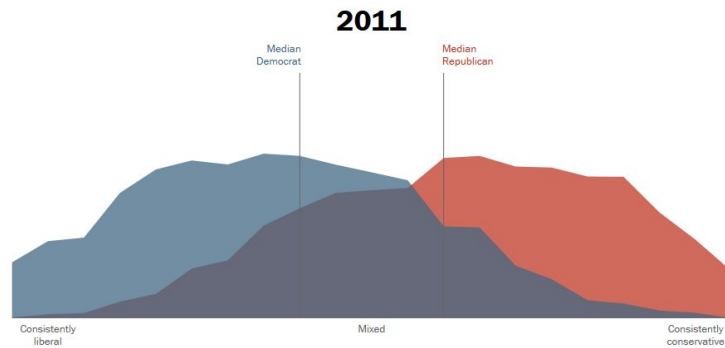
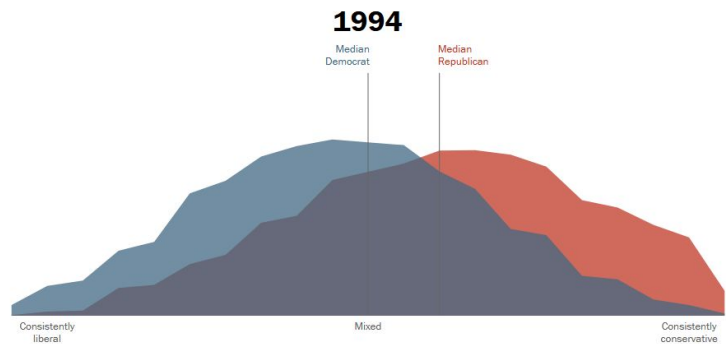
Modeling how tribalism and biased environments give rise to ideological distributions

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Motivation



Source: Pew Research (2017)

Overview



Political influence/polarization is extremely important, can we approach it mathematically?

Comprehensive theoretical framework for population ideology, integrating:

- Individual-level psychology
- Society-level media/information environment (systematically biased)
- Tribalism (partisan/identity-based bias)

Goals:

- Reproduces existing data (Pew, Bail et al. 2018)
- Able to incorporate (and inspire?) future data
- As “simple” as possible

Challenge: many different approaches, few compatible with each other



Basic Model Structure



1) Individuals react to what they see

- Function of the dissonance between a percept's ideology and their current ideology

2) What individuals see is systematically biased by their current position and party affiliation

- Probability distribution —> no assumption on influence type or structure

3) Individuals' reactions are modulated by tribalism

- Percepts and individuals have a 'party'. cross-party —> less 'trust'

How do people change ideology?

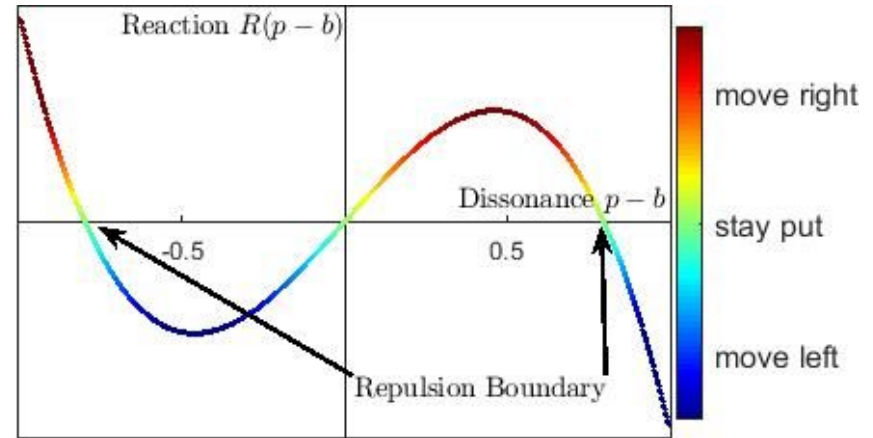
Continuous, finite ideology domain $[-1,1]$

- Current belief, b
- Percepts, p (subjectively rated)

“Reaction function”:

- local attraction, distal repulsion to ideas.
- “Repulsion Distance” d = distance at which percepts shift to being repulsive
 - Allows us to model tribalism: less accepting from out-group sources
- Repulsion is real: Bail et. al (2018)

Simple cubic reaction function:



$$R(p-b; d) = (p-b) \left[1 - \frac{(p-b)^2}{d^2} \right]$$

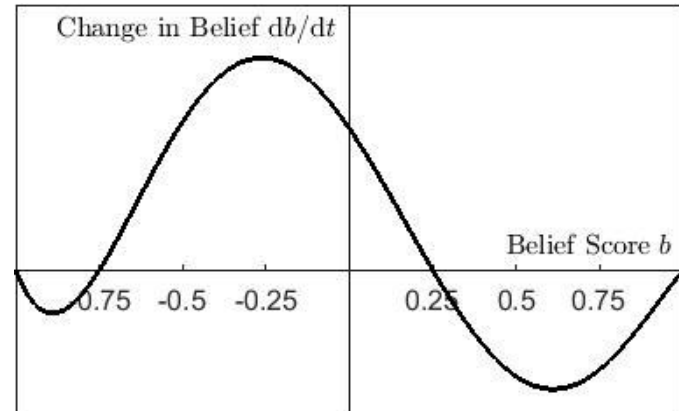
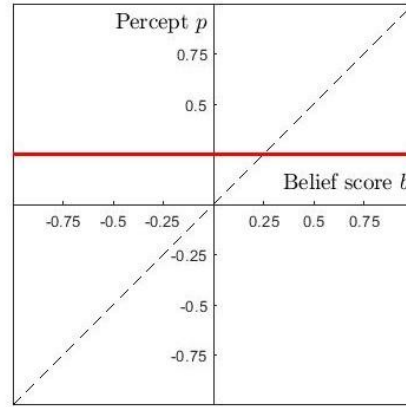
Simplest Case

- One repulsion distance d
- Constant “party line” percept shown to everyone

We can analytically determine how the whole population moves:

$$\tau \frac{db_j}{dt} = (1 - b_j^2) \left\{ (p_0 - b_j) \left[1 - \frac{(p_0 - b_j)^2}{d^2} \right] \right\}$$


Note: damped motion at edges to confine movement and represent “entrenchment”



Perception Curve

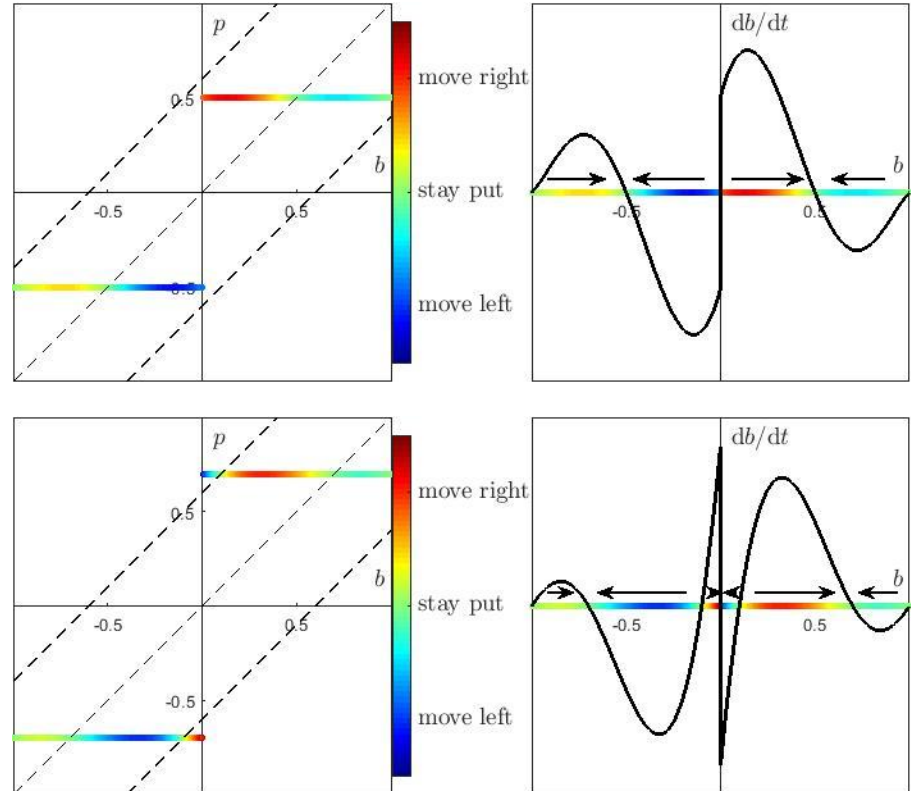
$$p = p(b)$$

- Current position determines percept diet

Graphical analysis technique

- 45° lines for $p=b$, $p=b \pm d$
- Crossings are fixed points
- Slope determines stability

—> Easy qualitative dynamics for ANY perception curve!



Inter-group Bias (Tribalism)

Adding another group (“party”)

- In-group perceptions p_i , repel distance d_i
- Out-group perceptions p_o , repel distance d_o
- Some fraction from in-group, $0 \leq f \leq 1$

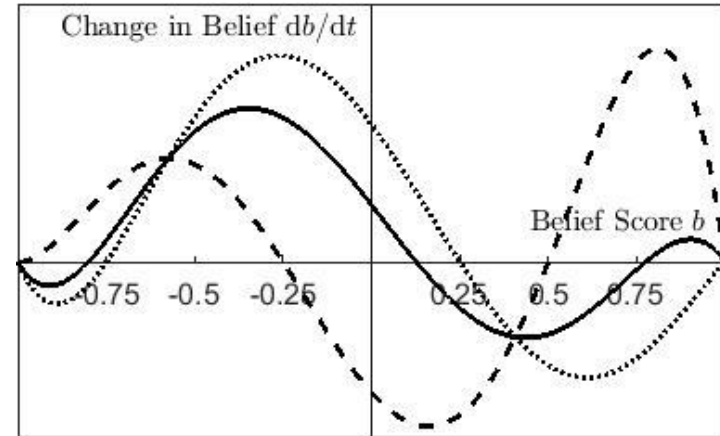
Movement = weighted average:

$$\tau \frac{db}{dt} = (1 - b^2) \left\{ f (p_i - b) \left[1 - \frac{(p_i - b)^2}{d_i^2} \right] + (1 - f)(p_o - b) \left[1 - \frac{(p_o - b)^2}{d_o^2} \right] \right\}$$

Looks complicated, but just linearly interpolated between results for each party independently

(back to constant “party line” for each)

$$p_i = 0.25, p_o = -0.25 \quad d_i = 1, d_o = 0.75 \quad f = 0.7$$



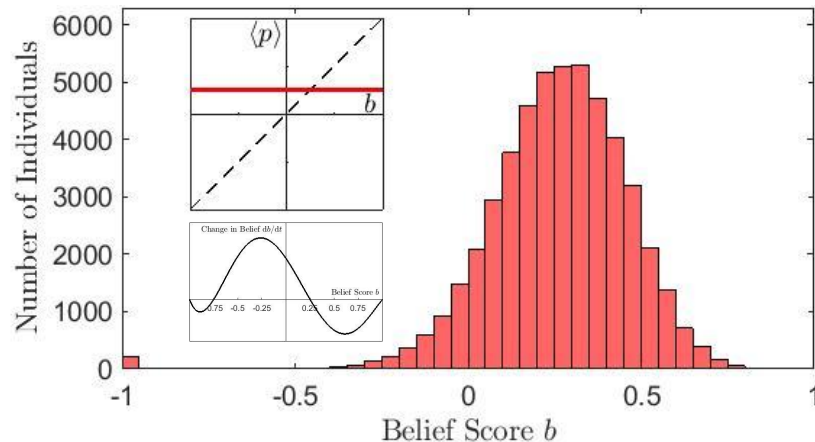
Adding Heterogeneity: Reactions

Reaction noise: differing impacts/reactions

- Normal noise $\rightarrow$ Itô SDE
- Attracting fixed points $\rightarrow$ stable distributions
- This noise is also edge-damped, to preserve asymptotic, entrenched extremes

'Simplest example', plus reaction noise:

$$\tau db = (1 - b^2) \left\{ (p - b) \left[1 - \frac{(p - b)^2}{d^2} \right] dt + \sigma_r dW \right\} \quad (\sigma_r = 0.25)$$



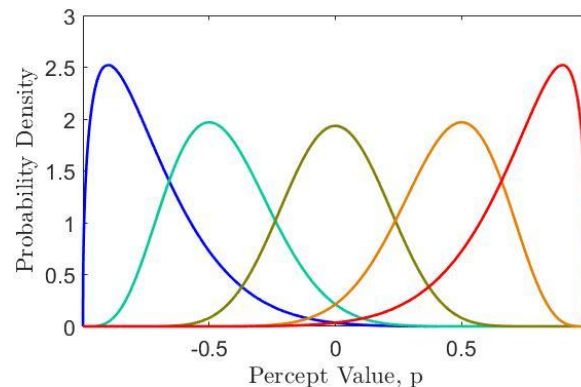
Adding Heterogeneity: Perceptions

Perception 'noise': distribution of sources/experiences

How to systematically parametrize?

- Beta distributions: bounded, 2 parameters
 - Perception curve $P(b)$ dictates *peak*
- One for each party, weighted by in-group fraction

$\sigma_p = 0.2$:



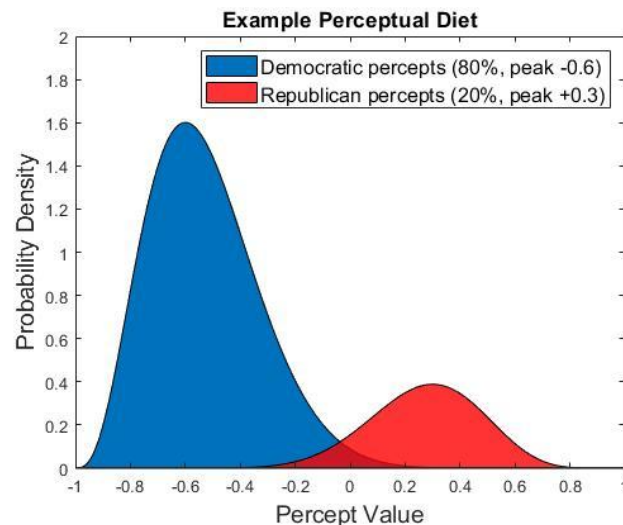
Adding Heterogeneity: Perceptions

Perception 'noise': distribution of sources/experiences

How to systematically parametrize?

- Beta distributions: bounded, 2 parameters
 - Perception curve $P(b)$ dictates *peak*
- One for each party, weighted by in-group fraction
- Total reaction = integral of these perception distributions against the (tribally-biased) reaction functions
 - Integral reflects assumption that percepts change on faster time scale than ideology

$$\sigma_p = 0.2:$$



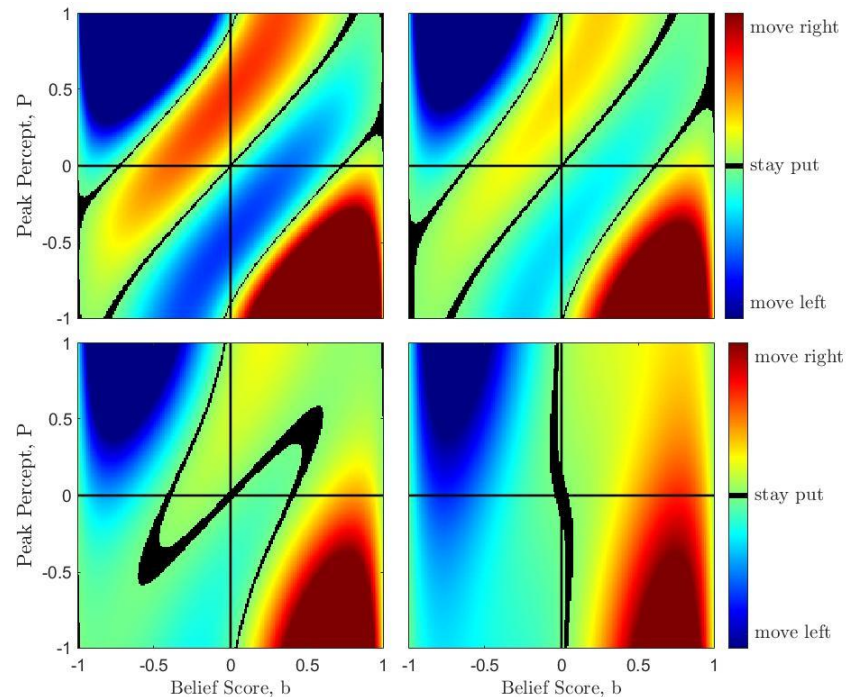
Reaction Maps

For any (global) repulsion distance d and percept distribution breadth σ_p , we can compute:

- Value at (b, P) = integral of reaction over percept distribution with peak (mode) P .
- Can use this for graphical analysis technique!

Note: d -dependent $\rightarrow$ separate maps for in-group content and out-group content

Bifurcation as noise increases $\rightarrow$ repulsion dominates



$d = 0.8$ $\sigma_p = 0.2, 0.3, 0.4, \text{ and } 0.5$

Full Model Structure

$$R(p - b; d) = (p - b) \left[1 - \frac{(p - b)^2}{d^2} \right]$$

$$v_{in} = \int_{-1}^1 R(p - b; d_{in}) \rho_{in}(p; b, \sigma_p) dp$$

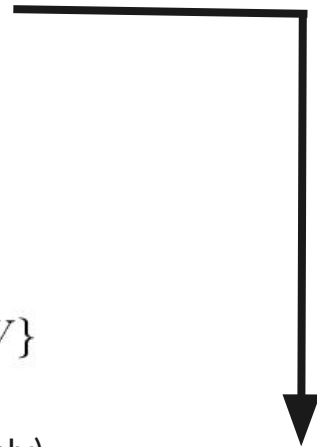
$$v_{out} = \int_{-1}^1 R(p - b; d_{out}) \rho_{out}(p; b, \sigma_p) dp$$

$$\tau db = (1 - b^2) \{ [f v_{in} + (1 - f) v_{out}] dt + \sigma_r dW \}$$

Parameters: $d_{in}, d_{out}, \sigma_p, \sigma_r, f$: arbitrary (chosen reasonably)

Perception curves P_{in}, P_{out} : arbitrary (fit)

$\mathcal{Q}_{in}, \mathcal{Q}_{out}$: beta distributions with peaks P_{in}, P_{out} and variance σ_p^2



Or use data!



Full Model: Matching Real-World Distributions

Perception curves

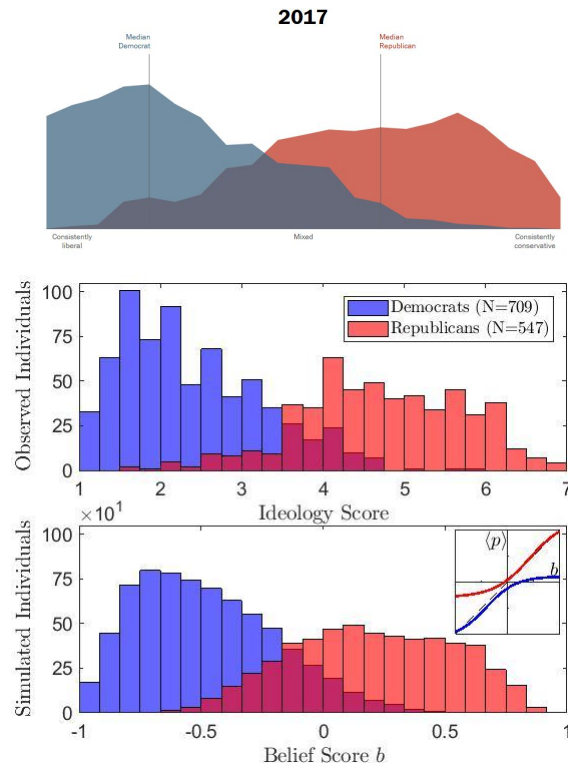
- $P(b)$ = sigmoid, one for each party

In-group fraction

- Rough “media bubble” effect:
 - $f_R(b) = 0.7 + 0.2b$ (Republicans)
 - $f_D(b) = 0.7 - 0.2b$ (Democrats)

Results:

- Equilibrium population distribution(s) matching real-world data
- Also reproduces *dynamics* results of Bail et. al (2018)!



Source: Pew Research (2017) (top), Bail et. al (2018) (middle)

Overview

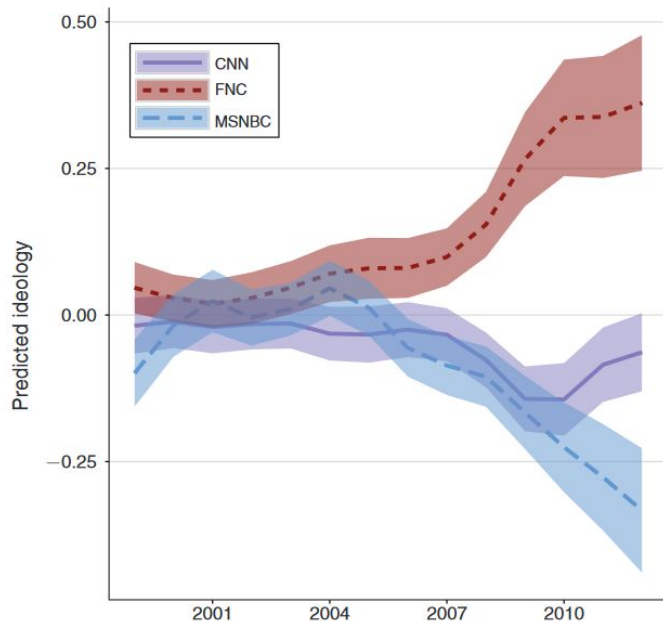
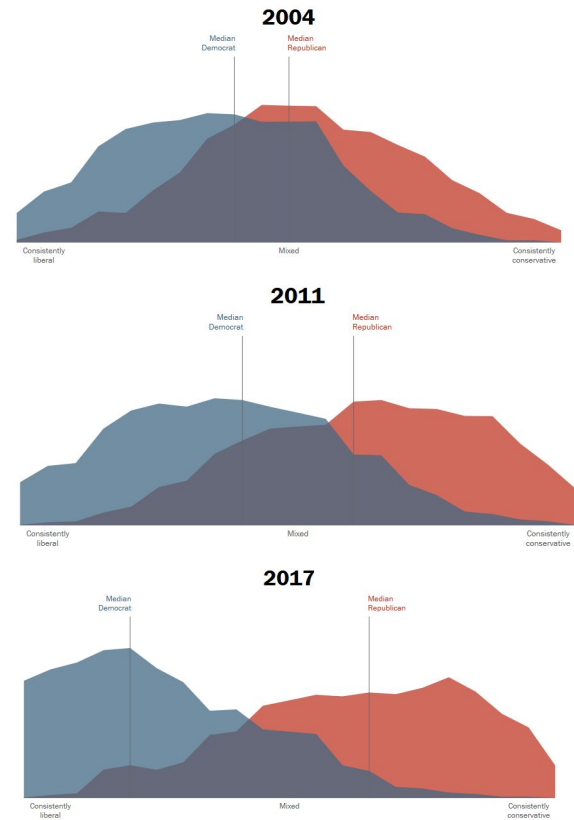


FIGURE 3. ESTIMATED IDEOLOGY BY CHANNEL YEAR

Martin/Yurukoglu (2017)



Overview

Reactions

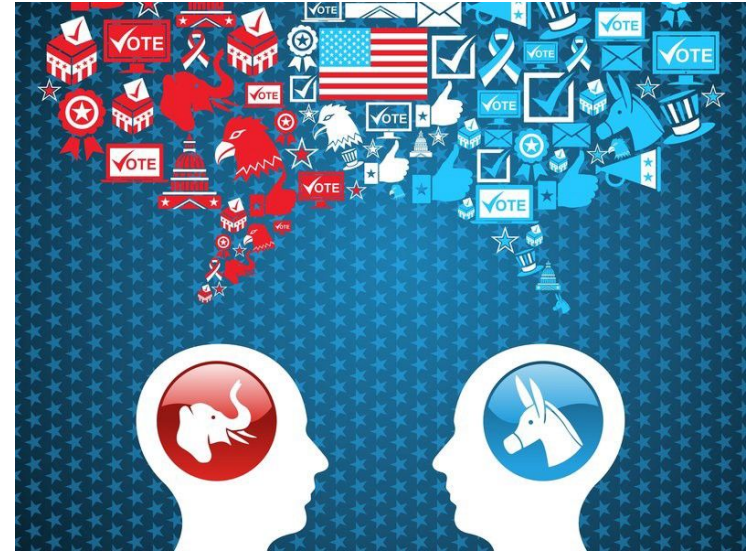
- Highly nonlinear psychological response

Perceptions

- Individuals coupled to systematically biased probabilistic environment
- Analogue for self-selecting, algorithmically-enabled, many-modal influence environments

Tribalism

- Identity mediates reaction
- Implies observed negative-campaigning, straw-manning persuasive tactics



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